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X-rays and Matter

Diffraction

Pair Distribution Function

Fourier Relationship

Converting Experimental Data

Examples

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PDFs at BXDS

Inclined Geometry PDF

Summary

CLS X-Ray Diffraction and Scattering Summer School 2023

Introduction to Pair Distribution Functions (PDF)

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August 17, 2023



What is the PDF Technique?

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The PDF method is a total scattering technique for determining local order in materials.



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1. Brief history of x-rays

2. How x-rays scatter through matter

3. X-ray diffraction

Overview

4. Pair Distribution Function Technique

- 5. Real Space Fourier Relationship
- 6. PDF Data Collection
- 7. Experimental Considerations
- 8. Developments in PDFs at BXDS-HEW
- 9. Final Remarks



A Brief History of x-ray Scattering

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- x-ray diffraction laws → Lawrence & William Henry Bragg (1912)
 Won Nobel Prize is 1914
- Powder x-ray diffraction measurements → Peter Debye & Paul Scherrer in Germany (1916) and Albert Hull in the United States (1917)
- ► Fourier Relationship between Debye scattering equation and real-space pair density derived → Zernicke & Prins (1927)
- ▶ First Pair Distribution Function (PDF) measurement → Debye & Menke (1930)
- First Synchrotron PDF measurement \rightarrow Takeshi Egami (1986)
 - $\blacktriangleright\,$ Datasets took ~ 12 hours to collect after days of setup
 - Energy sensitive point detector used
- ► PDF Measurements collected with an area detector → Peter Chupas & Xiangyun Qiu (2003)
 - PDF measurements are now done in the order of seconds.



X-ray Scattering on Electrons

in



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Elastic Scattering

 Coherently scattered photon has same phase and wavelength

phase and wavele Compton Scattering

- Photon imparts energy into the electron causing it to move
- Scattered Photon loses energy and has a larger wavelength
- Not useful for this work



X-ray Scattering on Atoms



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Momenum Transfer

$$Q = 4\pi\sin(\frac{2\theta}{2})/\lambda$$

Atomic Form Factor

- Photons scatter off the electron cloud
- Fewer scattering events with increasing momentum transfer
- Higher Z materials scatter x-rays more
- Distribution known as Atomic Form Factor
- The ratio of the coherent amplitude of waves scattered by an atom to that of a single electron



Diffraction with X-rays



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 $\mathsf{n}\lambda=2\mathsf{d}\sin(\theta)$



Non-crystalline scattering

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- Amorphous materials don't have repeating unit cells
 - No longer have nearly infinite planes leading to sharp bragg peaks
 - Diffuse scattering is the consistent short range ordering causing weak diffraction



Simulated XRD of Fe_3O_4



Measurement process



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The Pair Distribution Function

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$$G(r) = \frac{2}{\pi} \int \mathsf{Q}(S(\mathsf{Q}) - 1) \sin(\mathsf{Qr}) \mathsf{d}\mathsf{Q}$$

$$Q = \frac{4\pi}{\lambda} \sin\left(\frac{2\theta}{2}\right)$$





Other Forms

 $R(r) = 4\pi r^2 \rho_0 g(r)$

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Reciprocal and Real Space



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Effects of Finite limit of Reciprocal Space

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How Real Space correlates to Reciprocal Space





Single Peak



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Two Peaks



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Three Peaks Canadian Centre canadien de ravonnement



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Integrated Data





Normalizing to Atomic Form Factor





$\mathsf{S}(\mathsf{Q}) \to \mathsf{F}(\mathsf{Q}) = \mathsf{Q}(\mathsf{S}(\mathsf{Q}) \text{ - } 1)$





$F(Q) \rightarrow G(r) = \frac{2}{\pi} \int F(Q) \sin(Qr) dQ$



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$\mathsf{G}(\mathsf{r}) \rightarrow \mathsf{R}(\mathsf{r}) = \mathsf{r}\mathsf{G}(\mathsf{r}) + 4\pi\rho_0 r^2$





Nanoparticles



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Local Ordering

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Experimental Challenges

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- Q max vs resolution Unwanted Photons
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- Q-range & Q-resolution
- Sample quality
- Compton Scattering
- Non-sample coherent scattering
- Detector noise

The Q Problem



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Sample-Detector Distance



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Sample-Detector Distance



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60 keV 70 70 keV 60 50 Q(Å⁻¹) 40 30 20 10 0 20 40 60 80 100 140 120 160 180 0 2θ(°)

Q Related to Angle and Energy





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Non-Sample Signal







High Energy Wiggler Beamline (BXDS-HEW)

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Details

- 20-95 keV
- Rapid Powder XRD
- Pair Distribution Function Measurement
- High Pressure XRD
- Resistive furnace cells with gas flow for in-situ measurements (RT ≤ T ≤ 1000C)
- Cold air stream (80 K ≤ T ≤ 500 K)



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User Pro Tips

- What are you hoping to resolve?
 - Short range structure
 - Medium range ordering
 - Comparitive changes (in situ/ in operando)
 - Modeling
- Is there low Q or high Q signal?
- Be aware of the experimental parameters
 - Choice of energy vs flux and Q
 - Area detector being used
 - Pixel Size
 - Afterglow
 - Dark current
 - Flatfield
 - Saturation levels
 - Beam size
 - Collect more subtractive images than you need!



Improving PDF Collection



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Inclined Geometry

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XPixels

Advantages

- ► Higher Q accessed
- Better Q resolution for low angle peaks & lower resolution for high angle peaks improves dynamic range
- Can use much lower x-rav energies for equivalent Q



Inclined Geometry

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Disadvantages

- Geometry calibration much harder
- High Q signal very weak noise can easily get convoluted
- New software needed to accurately work in these extremes
- No averaging over full rings need good smooth samples
- Background measurements needed more frequently



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Comparison

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N. Burns et al., Journal of Applied Crystallography 2023, 56, 510.



Ru_5CI_{12} Nanoparticle PDF Measurement



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Summarv

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- PDF is a powerful tool that can probe local structure regardless of crystallinity
- With synchrotrons data collection is fast to observe structural changes as they happen
- PDF methods are improving and provide a way of seeing local structure nanoparticle structure
- GSAS-II very useful for PDF generation but it's not difficult to make your own code



Brockhouse Team

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Thank You

Resources

- X-Ray Diffraction B. E. Warren (1990)
- Elements of X-Ray Diffraction B. D. Cullity (2001)
- The rise of the X-ray atomic pair distribution function method: a series of fortunate events - S. Billinge https://doi.org/10.1098/rsta.2018.0413
- An inclined detector geometry for improved X-ray total scattering measurements – N. Burns *et al* https://doi.org/10.1107/S1600576723001747
- GSAS-II https://subversion.xray.aps.anl.gov/trac/pyGSAS