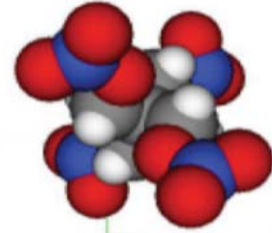


RIGID BODIES IN GSAS-II: WHY, WHAT AND HOW

GSAS-2



BRIAN TOBY
Senior Scientist



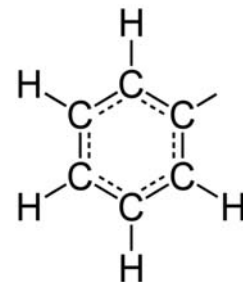
WHY USE CONSTRAINTS?

Reason #1. Structure refinement

Frequently, particularly with powder diffraction, one does not have enough data to independently determine the position of every non-hydrogen atom at the expected level of accuracy.

Use of constraints allows a crystallographic model to be simplified to be consistent with what has been measured.

Example: the 6 C atoms in a phenyl group (C_6H_5) offer 18 degrees of freedom, but if the group's internal geometry is fixed, only 6 (or less) degrees need to be treated, plus the fit structure will be more reasonable since the internal geometry of a phenyl group is well-known and does not change.



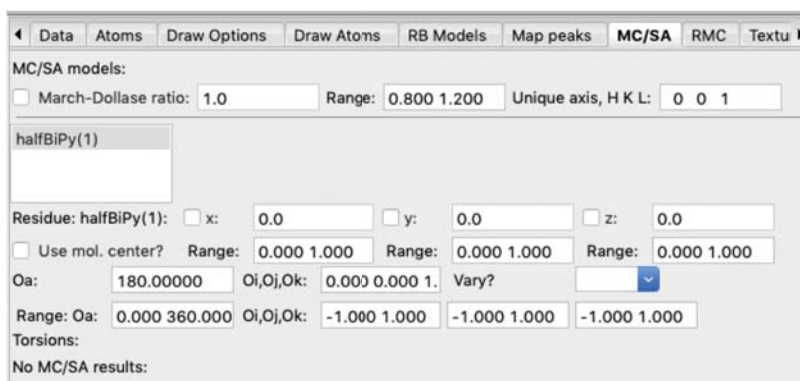
<https://commons.wikimedia.org/wiki/File:Phenyl-group-2D-flat.png#/media/File:Phenyl-group-2D-flat.png>

Note: when too many parameters are varied, the model will be “overfit.” Unreasonable results are obtained because the data are not sufficient to independently determine all the terms that are being fit. “Fitting to noise.”

WHY USE RIGID BODIES?

Reason #2. Structure solution

- When a structure must be solved, the complexity of that problem can be huge if every atom is considered as an independent entity. However, often large portions of the structure have known internal geometries and can be treated as groups where the group has only an unknown location and/or orientation. Sometimes a few torsional parameters may unknown and can also be included.
- Rigid bodies can be used with the Monte-Carlo/Simulated Annealing structure solution module (see the MC/SA tab in the Phase panel.)



WHAT ARE RIGID BODIES?

Rigid bodies require two sets of axes.

1. *the usual set of crystallographic coordinates (along a, b & c) and*
2. *Cartesian axes, internal to the body*

Rigid body parameters set the relation of these coordinate systems.

- Atom positions inside rigid bodies are specified in Cartesian coordinates, relative to an origin.
- Rigid bodies will be placed inside a crystal structure with *at most* 6 degrees of freedom externally: 3 coordinates for the origin location and 3 orientation parameters. Symmetry may fix some of these.
- Group motion (TLS) terms for rigid bodies can be used generate to treat atomic displacement parameters (“thermal motion”) for the atoms in the group.
- GSAS-II allows additional internal degrees of freedom in rigid bodies:
 1. **Vector rigid bodies:** offers grouped bond lengths
 2. **Residue rigid bodies:** offers torsion angles

HOW DOES GSAS-II IMPLEMENT RIGID BODIES?

Option 1: Vector bodies

- Vector rigid bodies have fixed geometries, but optionally allow for one or more scaling parameters
 - The scaling parameters can be refined (but can be fixed).
- The scaling parameters determine size factors for the rigid body and typically define bond lengths.
- In vector rigid body a set of atom positions (r_j) are generated from coordinates $v_{j,k}$

$$r_j = t_1 \cdot v_{j,1} + t_2 \cdot v_{j,2} + \dots$$

or equivalently

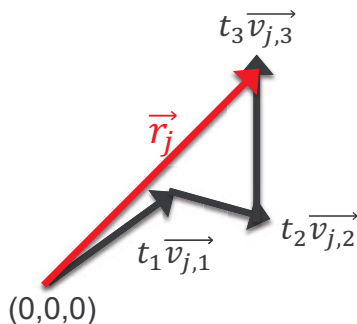
$$\begin{bmatrix} \bar{r}_1 \\ \bar{r}_2 \\ \bar{r}_3 \\ \cdot \\ \cdot \\ \cdot \\ \bar{r}_n \end{bmatrix} = t_1 \begin{bmatrix} \bar{v}_{1,1} \\ \bar{v}_{2,1} \\ \bar{v}_{3,1} \\ \cdot \\ \cdot \\ \cdot \\ \bar{v}_{n,1} \end{bmatrix} + t_2 \begin{bmatrix} \bar{v}_{1,2} \\ \bar{v}_{2,2} \\ \bar{v}_{3,2} \\ \cdot \\ \cdot \\ \cdot \\ \bar{v}_{n,2} \end{bmatrix} + \dots$$

VECTOR RIGID BODIES: CONCEPT

A sum of vectors provides the position of each atom

- A concept that explains both the name and reasoning that helps understand how vector bodies work is to consider that each atom position is generated relative to the origin from the sum of a scaled set of vectors:

$$\vec{r}_j = t_1 \vec{v}_{j,1} + t_2 \vec{v}_{j,2} + t_3 \vec{v}_{j,3} + \dots$$



$$\begin{bmatrix} \bar{r}_1 \\ \bar{r}_2 \\ \bar{r}_3 \\ \cdot \\ \cdot \\ \cdot \\ \bar{r}_n \end{bmatrix} = t_1 \begin{bmatrix} \bar{v}_{1,1} \\ \bar{v}_{2,1} \\ \bar{v}_{3,1} \\ \cdot \\ \cdot \\ \cdot \\ \bar{v}_{n,1} \end{bmatrix} + t_2 \begin{bmatrix} \bar{v}_{1,2} \\ \bar{v}_{2,2} \\ \bar{v}_{3,2} \\ \cdot \\ \cdot \\ \cdot \\ \bar{v}_{n,2} \end{bmatrix} + \dots$$

FICTITIOUS VECTOR RB EXAMPLE

Vector example: part 1A

- Imagine a square rigid body with 8 atoms
 - for simplicity $z (=0 \text{ for all atoms})$ is omitted here.

Coordinates for A:

$(0.5,0.5), (0.5,-0.5), (-0.5,-0.5), (-0.5,0.5)$

- A-A distance is 1

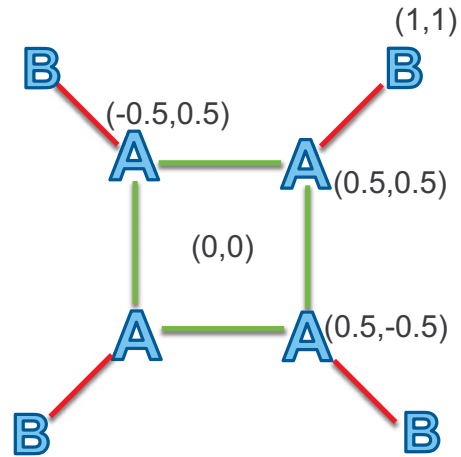
Coordinates for B:

$(1,1), (1,-1), (-1,-1), (-1,1)$

- A-B distance is $1/\sqrt{2}$

This can be expressed as a single matrix:

$$\begin{pmatrix} r_1 \\ r_2 \\ \vdots \\ r_8 \end{pmatrix} = \begin{pmatrix} 0.5 & 0.5 \\ -0.5 & 0.5 \\ -0.5 & -0.5 \\ 0.5 & -0.5 \\ 1 & 1 \\ -1 & 1 \\ -1 & -1 \\ 1 & -1 \end{pmatrix}$$



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FICTITIOUS VECTOR RB EXAMPLE

Vector example: part 1B

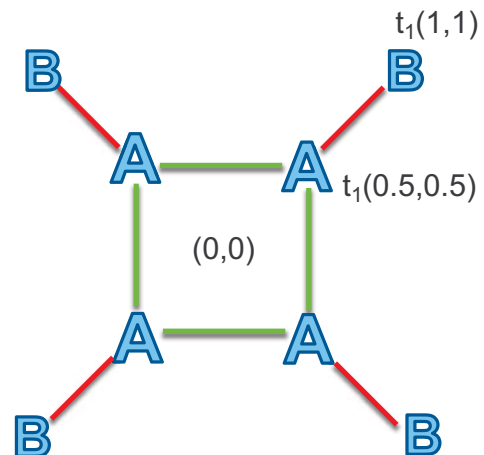
- Single matrix with scaling factor :

$$\begin{pmatrix} r_1 \\ r_2 \\ \vdots \\ r_8 \end{pmatrix} = t_1 \begin{pmatrix} 0.5 & 0.5 \\ -0.5 & 0.5 \\ -0.5 & -0.5 \\ 0.5 & -0.5 \\ 1 & 1 \\ -1 & 1 \\ -1 & -1 \\ 1 & -1 \end{pmatrix}$$

Note that t_1 scales the entire rigid body

- A-A bonds are length t_1
- A-B bonds are length $t_1/\sqrt{2}$

Arbitrary units can be used for coordinates since t_1 scales them to Ångstroms.



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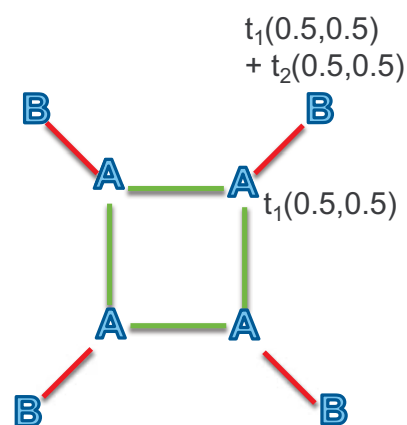
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FICTITIOUS VECTOR RB EXAMPLE

Vector example: part 2

- With two matrices we can make A-A and A-B lengths into separate variables:

$$\begin{pmatrix} r_1 \\ r_2 \\ \vdots \\ r_8 \end{pmatrix} = t_1 \begin{pmatrix} 0.5 & 0.5 \\ -0.5 & 0.5 \\ -0.5 & -0.5 \\ 0.5 & -0.5 \\ 0.5 & 0.5 \\ -0.5 & 0.5 \\ -0.5 & -0.5 \\ 0.5 & -0.5 \end{pmatrix} + t_2 \begin{pmatrix} 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0.5 & 0.5 \\ -0.5 & 0.5 \\ -0.5 & -0.5 \\ 0.5 & -0.5 \end{pmatrix}$$



Note that t_1 scales the entire rigid body; A & B atoms all move with t_1

Note that only B atoms move with t_2

- A-A bonds are length t_1
- A-B bonds are length $t_2/\sqrt{2}$

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HOW DOES GSAS-II IMPLEMENT RIGID BODIES?

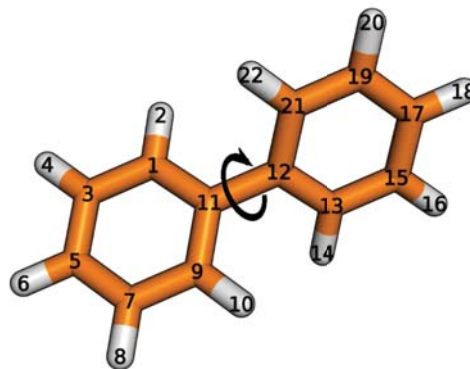
2. Residue rigid bodies

The dimensions of a residue rigid body cannot change, but there can be torsion angles defined, which allow sections of the molecule to reposition. There can be multiple torsions in a rigid body.

Example: this biphenyl [(C₆H₅)₂] molecule has one potential *internal* degree of freedom which is the torsional angle on the C-C bond joining the two rings (atoms 11 & 12 in diagram)

Residue coordinates must be in Ångstroms

When defining torsions, GSAS-II needs two atoms to be defined: an origin and a pivot atom. Other atoms bonded to the pivot are called riders.



Torsion origin: 11, pivot 12, riders 13 & 21
(or equivalently, origin: 12, pivot: 11, riders: 1 & 9)

<http://erg.biophys.msu.ru/tiki/tiki-index.php?page=Ab+initio+energy+scan>

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METHODS TO GENERATE RIGID BODY COORDINATES

There are several approaches for generating rigid body coordinates.

1. For simple 2-D bodies, the object can be sketched out on paper and the coordinates can be derived from simple geometry.
2. A molecular editor, force-field or quantum code* can be used to build and minimize the approximate (gas phase) structure for a molecule or fragment. Cartesian coordinates are then exported.
 - The open source Avogadro program is a good choice (<https://sourceforge.net/projects/avogadro/>); write XYZ output.
3. If you have a crystal structure (for example, from CSD) containing the rigid body you wish to use, those atoms can be extracted into a GSAS-II rigid body.
 - You can extract atoms from a structure and then optimize in Avogadro

* Note that GSAS-II will not read a Z-matrix file (which is commonly used for simulations) but OpenBabel (<http://openbabel.org>) will convert this to XYZ output format.

SYMMETRY AND RIGID BODIES

Before defining a rigid body, it is important to consider how those atoms will appear in the model. Symmetry can place constraints on the rigid body origin and axial orientation *in Cartesian space* and dictate how the RB is constructed.

- Is there internal symmetry to the rigid body? If so, is that symmetry enforced by the space group symmetry in the lattice?
 - For the example that follows, we will have a rigid body on a center of symmetry (-1) site. This means that the Cartesian origin must be placed at the crystallographic site where the -1 is located.
 - More details on symmetry and rigid bodies will be covered later
- Note that a single rigid body may be inserted in multiple locations in a single structure, but if the moiety is found in different symmetry environments, the body might need to be defined with more than one description.

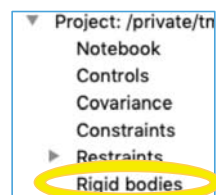
If TLS parameters will be refined, it is best to put the origin at the center of mass

HOW ARE RIGID BODIES USED IN GSAS-II?

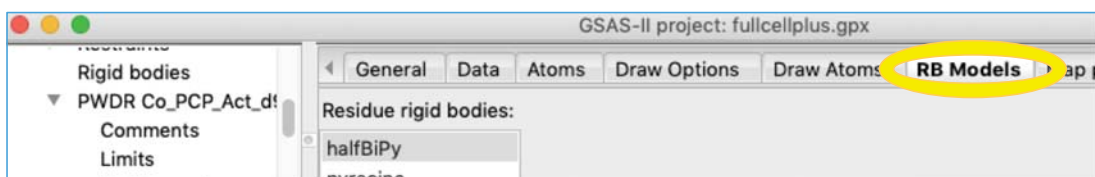
Two steps are needed for rigid bodies

Create: Bodies are first defined for a project

- Define atom positions, Cartesian origin & axes. This is done in the “Rigid bodies” tree item



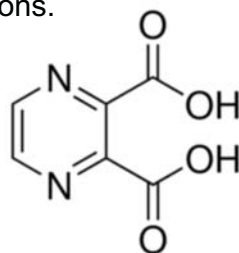
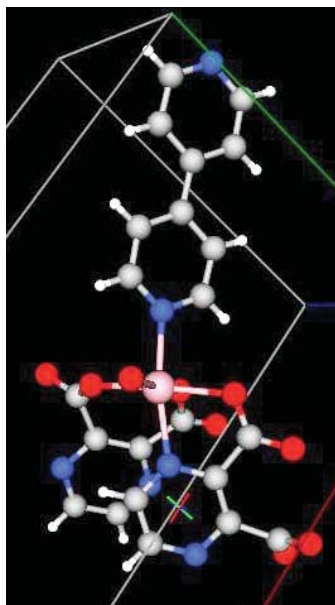
Insert: The defined rigid body is placed into a crystal structure, defining the position of the group and its orientation. Inserting a body also defines which atoms in the structure will have their coordinates generated from the body. This is done in the “RB Models” phase tab.



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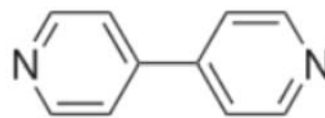
TWO RB EXAMPLES IN ONE MOF STRUCTURE

- The pictured structure is built from a metal ion, 4-4'-bipyridine molecules, and 2,3-pyrazinedicarboxylic acid ions.



2,3-pyrazinedicarboxylic acid

<https://www.sigmaaldrich.com/catalog/product/aldrich/p56208?lang=en®ion=US>



4-4'-bipyridine

The asymmetric unit contains

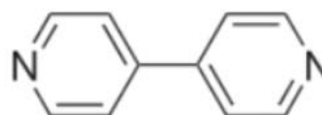
- a half 4-4'-bipyridine (bipyridine)
- a single complete 2,3-pyrazinedicarboxylic acid ion (pyrazine)

The symmetry of each needs to be considered separately

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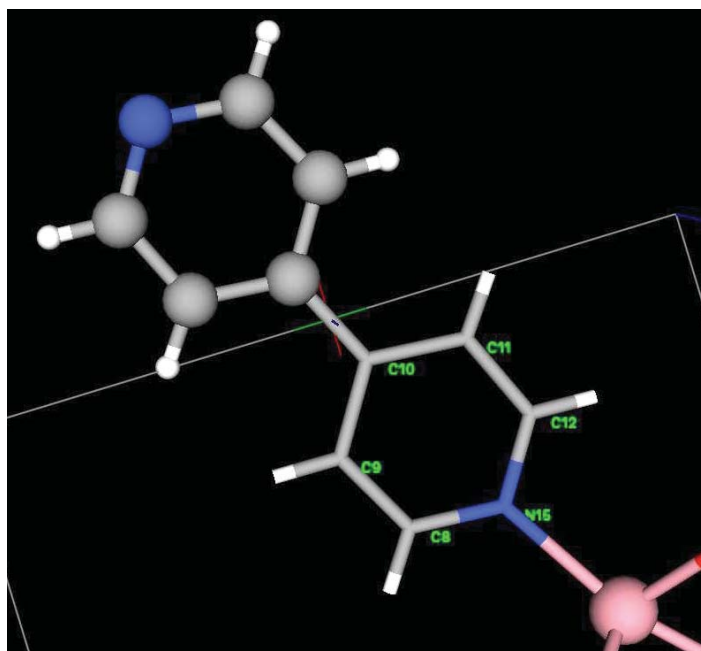
4-4'-BIPYRIDINE (BIPYRIDINE)

Care required: this is on a special position



- The asymmetric unit is drawn as stick figure & labeled (symmetry-generated atoms are ball-and-stick)
- Note that there is a center of symmetry ($\bar{1}$) between C10 and its symmetry-twin.
- Examination of plot or coordinates identifies the $\bar{1}$ location as $(0, \frac{1}{2}, 1)$

To preserve the symmetry, the origin for the rigid body must be at the midpoint between C10 and C10'. That will be placed at $(0, \frac{1}{2}, 1)$ in crystal coordinates.



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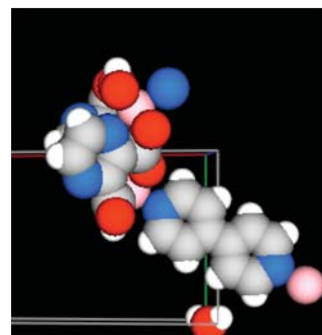
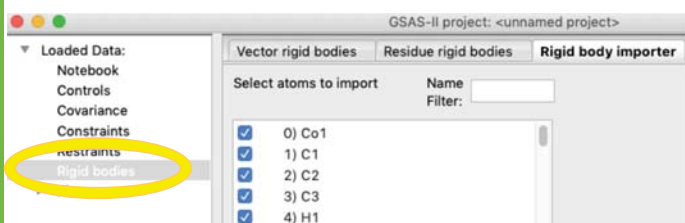
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CREATE THE BIPYRIDINE RIGID BODY (1)

Work can be done in a new project, but a phase is needed to create the “Rigid Bodies” tree entry

In this example we will use a publication as the source of coordinates for the rigid body.

- Note that because we will need both C10 and C10' to establish the origin, the structure must be expanded to provide both atoms before it is read in.
- From either “Vector rigid bodies” or “Residue rigid bodies” use the Edit Vector Body/Extract from file menu command
- Select a file format, in this case CIF and then find the CIF file and select it
 - All atoms are brought into the “Rigid body importer” selector and are plotted.

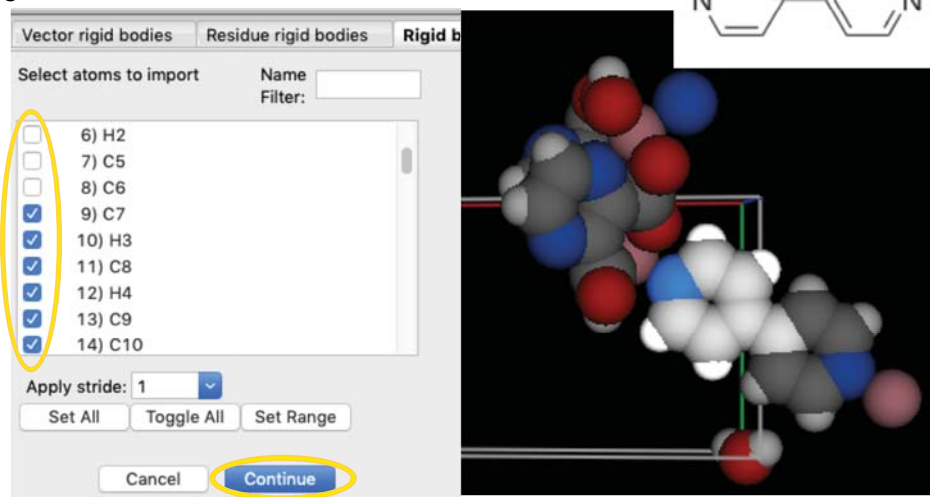


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CREATE THE BIPYRIDINE RIGID BODY (2)

Select the atoms needed to build the rigid body

- In the Atom selector, unselect all atoms, and select only the atoms from one ring plus one atom on the other ring.
 - Note that selected atoms are brightly colored while unselected atoms appear much darker.
- Press continue



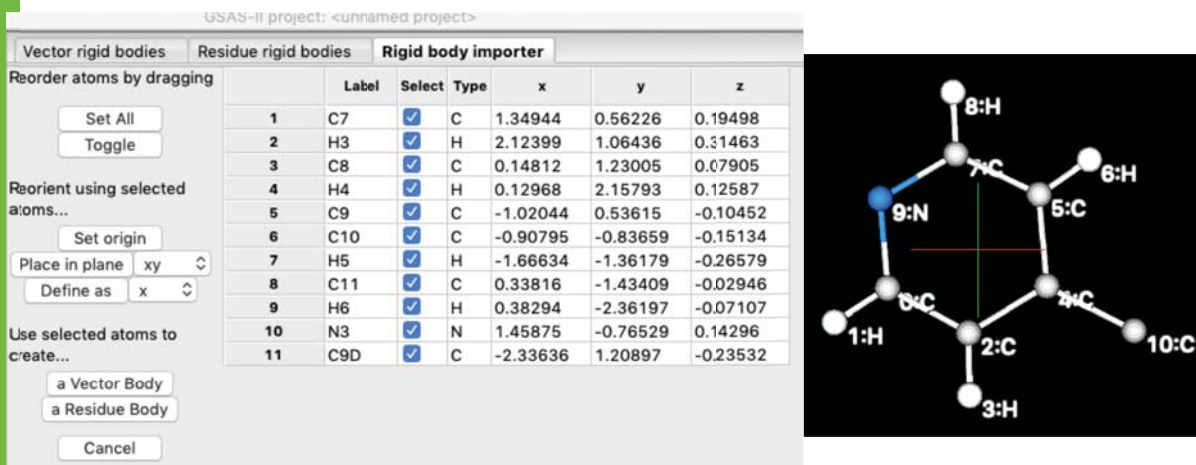
The screenshot shows the 'Rigid body importer' dialog box with the 'Select atoms to import' list. Atoms 9) C7, 10) H3, 11) C8, 12) H4, 13) C9, and 14) C10 are selected. The 'Continue' button is highlighted. To the right is a 3D ball-and-stick model of bipyrindine with a 2D chemical structure inset above it.

Label	Select	Type	x	y	z
6) H2	<input type="checkbox"/>	H			
7) C5	<input type="checkbox"/>	C			
8) C6	<input type="checkbox"/>	C			
9) C7	<input checked="" type="checkbox"/>	C			
10) H3	<input checked="" type="checkbox"/>	H			
11) C8	<input checked="" type="checkbox"/>	C			
12) H4	<input checked="" type="checkbox"/>	H			
13) C9	<input checked="" type="checkbox"/>	C			
14) C10	<input checked="" type="checkbox"/>	C			

CREATE THE BIPYRIDINE RIGID BODY (3)

For convenience (but not required) we will define the axes orientation

Once the atoms are selected, a new table with Cartesian coordinates and a plot of the atoms is shown.



The screenshot shows the 'Rigid body importer' dialog box with the 'Rigid body importer' tab selected. The 'Reorder atoms by dragging' section is active, and the 'Rigid body importer' table is displayed. The table shows the Cartesian coordinates for the selected atoms. To the right is a 3D plot of the atoms with labels for each atom.

Label	Select	Type	x	y	z
1	<input checked="" type="checkbox"/>	C	1.34944	0.56226	0.19498
2	<input checked="" type="checkbox"/>	H	2.12399	1.06436	0.31463
3	<input checked="" type="checkbox"/>	C	0.14812	1.23005	0.07905
4	<input checked="" type="checkbox"/>	H	0.12968	2.15793	0.12587
5	<input checked="" type="checkbox"/>	C	-1.02044	0.53615	-0.10452
6	<input checked="" type="checkbox"/>	C	-0.90795	-0.83659	-0.15134
7	<input checked="" type="checkbox"/>	H	-1.66634	-1.36179	-0.26579
8	<input checked="" type="checkbox"/>	C	0.33816	-1.43409	-0.02946
9	<input checked="" type="checkbox"/>	H	0.38294	-2.36197	-0.07107
10	<input checked="" type="checkbox"/>	N	1.45875	-0.76529	0.14296
11	<input checked="" type="checkbox"/>	C	-2.33636	1.20897	-0.23532

CREATE THE BIPYRIDINE RIGID BODY (4)

Put atoms in plane (optional)

With all atoms selected, click on the place in plane, with “xy” selected adjacent. Note that the z values are nearly zero. There is no visible change in the plot except that the cross hairs rotate, showing the different axes directions.

Reorder atoms by dragging

Set All
Toggle

Reorient using selected atoms...

Set origin
Place in plane xy
Define as x

Use selected atoms to create...

a Vector Body
a Residue Body
Cancel

	Label	Select	Type	x	y	z
1	C7	<input checked="" type="checkbox"/>	C	1.35977	0.57110	0.19498
2	H3	<input checked="" type="checkbox"/>	H	2.14013	1.07844	0.31463
3	C8	<input checked="" type="checkbox"/>	C	0.14933	1.23245	0.07905
4	H4	<input checked="" type="checkbox"/>	H	0.13121	2.16151	0.12587
5	C9	<input checked="" type="checkbox"/>	C	-1.02875	0.53042	-0.10452
6	C10	<input checked="" type="checkbox"/>	C	-0.91462	-0.84298	-0.15134
7	H5	<input checked="" type="checkbox"/>	H	-1.67817	-1.37313	-0.26579
8	C11	<input checked="" type="checkbox"/>	C	0.34058	-1.43382	-0.02946
9	H6	<input checked="" type="checkbox"/>	H	0.38547	-2.36262	-0.07107
10	N3	<input checked="" type="checkbox"/>	N	1.46983	-0.75741	0.14296
11	C9D	<input checked="" type="checkbox"/>	C	-2.35478	1.19605	-0.23532

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CREATE THE BIPYRIDINE RIGID BODY (5)

Set up the axes (optional)

We will make the x-axis run from the N atom to one of the C atoms by unselecting the N atom and then toggle (so that it is the only selected atom). Temporarily make that atom the origin by pressing the “Set origin” button. Note that the cross hairs move to the N atom and its coordinates are now (0,0,0).

Then unselect the N atom and select the C atom and press “define as” with “x” selected. The body rotates and the selected C atom is now at (x,0,0)

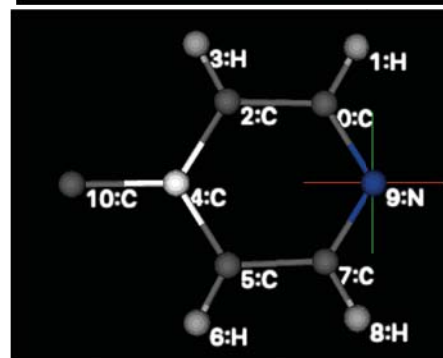
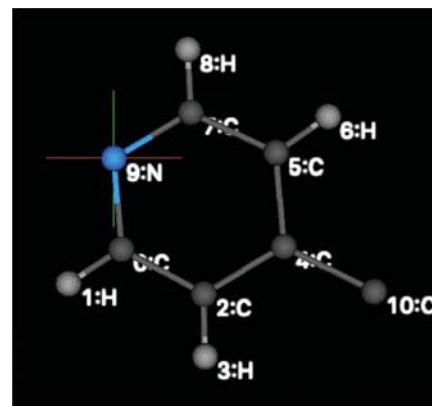
Reorder atoms by dragging

Set All
Toggle

Reorient using selected atoms...

Set origin
Place in plane xy
Define as x

	Label	Select	Type	x	y	z
1	C7	<input type="checkbox"/>	C	0.70648	-1.13046	0.00170
2	H3	<input type="checkbox"/>	H	0.24528	-1.93893	0.00025
3	C8	<input type="checkbox"/>	C	2.08541	-1.16375	0.00387
4	H4	<input type="checkbox"/>	H	2.52715	-1.98126	0.00823
5	C9	<input checked="" type="checkbox"/>	C	2.81094	0.00000	-0.00000
6	C10	<input type="checkbox"/>	C	2.08028	1.16849	0.00522
7	H5	<input type="checkbox"/>	H	2.51608	1.98954	0.01093
8	C11	<input type="checkbox"/>	C	0.69387	1.11861	0.00003
9	H6	<input type="checkbox"/>	H	0.22844	1.92363	-0.00244
10	N3	<input type="checkbox"/>	N	0.00000	0.00000	0.00000
11	C9D	<input type="checkbox"/>	C	4.29458	0.01585	0.00141

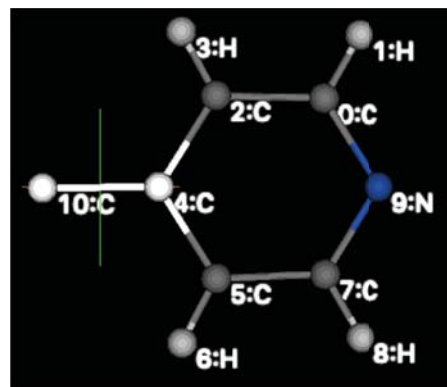


CREATE THE BIPYRIDINE RIGID BODY (6)

Required: place origin on center of symmetry

The midpoint between the two rings *must* be the location of the center of symmetry.

Select the two C atoms that join the two rings. Then press the “Set origin” button to put the origin at the average of the two selected positions.



Reorder atoms by dragging		Label	Select	Type	x	y	z
<input type="button" value="Set All"/>	1	C7	<input type="checkbox"/>	C	-2.84628	-1.13838	0.00099
<input type="button" value="Toggle"/>	2	H3	<input type="checkbox"/>	H	-3.30748	-1.94686	-0.00046
	3	C8	<input type="checkbox"/>	C	-1.46735	-1.17167	0.00316
Reorient using selected atoms...	4	H4	<input type="checkbox"/>	H	-1.02561	-1.98919	0.00753
<input type="button" value="Set origin"/>	5	C9	<input checked="" type="checkbox"/>	C	-0.74182	-0.00793	-0.00071
Place in plane <input type="button" value="xy"/>	6	C10	<input type="checkbox"/>	C	-1.47248	1.16056	0.00452
Define as <input type="button" value="x"/>	7	H5	<input type="checkbox"/>	H	-1.03668	1.98162	0.01023
	8	C11	<input type="checkbox"/>	C	-2.85889	1.11068	-0.00067
Use selected atoms to create...	9	H6	<input type="checkbox"/>	H	-3.32432	1.91571	-0.00315
<input type="button" value="a Vector Body"/>	10	N3	<input type="checkbox"/>	N	-3.55276	-0.00793	-0.00071
	11	C9D	<input checked="" type="checkbox"/>	C	0.74182	0.00793	0.00071

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CREATE THE BIPYRIDINE RIGID BODY (7)

Export all atoms in the ring, but not the “extra” atom

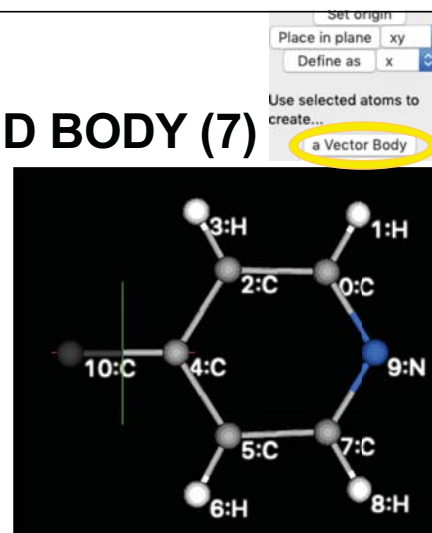
We want to export all but the last C atom (C11). (This can be done simply by unselect the 4th atom and press toggle, highlighting all atoms in the one ring.)

Then create a residue rigid body by pressing the “a Residue Body” button.

Change the name of the body

If you will use the body in a different project, use “Edit Rigid Body”/“Save rigid body” to write a file.

Note: while we will use a residue body here, since there are no torsions for this body, a vector rigid body would work just as well.



Vector rigid bodies		Residue rigid bodies			
Residue name:	half-bipy	Plot	Delete	Strip H-atoms	
Orientation reference non-H atoms A-B-C: C7 H3 C8					
Name	Type	Cart x	Cart y	Cart z	
0	C7	C	-2.84628	-1.13838	0.00099
1	H3	H	-3.30748	-1.94686	-0.00046
2	C8	C	-1.46735	-1.17167	0.00316
3	H4	H	-1.02561	-1.98919	0.00753
4	C9	C	-0.74182	-0.00793	-0.00071
5	C10	C	-1.47248	1.16056	0.00452
6	H5	H	-1.03668	1.98162	0.01023
7	C11	C	-2.85889	1.11068	-0.00067
8	H6	H	-3.32432	1.91571	-0.00315
9	N3	N	-3.55276	-0.00793	-0.00071

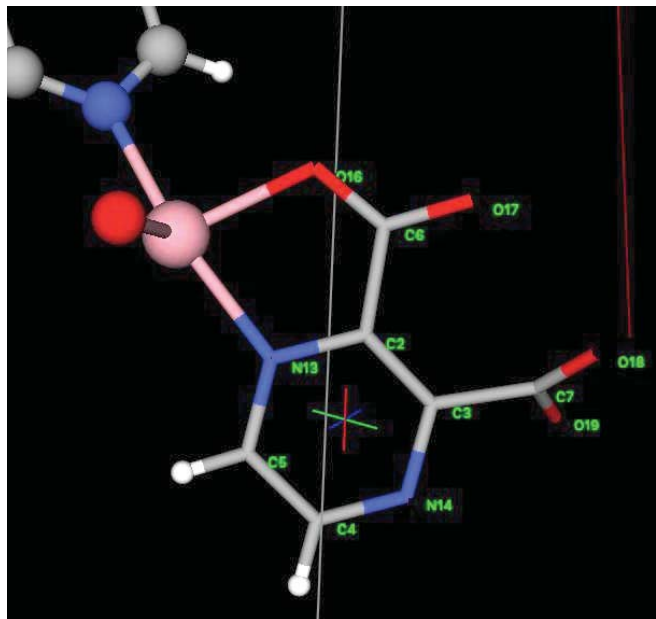
INSERT THE 2,3-PYRAZINEDICARBOXYLIC ACID (PYRAZINE)

Note: not on a special position

The asymmetric unit structure has been drawn here

- Pyrazine asymmetric unit drawn as stick figure & labeled
- Note that the ion is planar with the exception of the 4 oxygens
 - The O atoms will need torsions to position them

There is no internal symmetry here so the origin of the body can be arbitrary

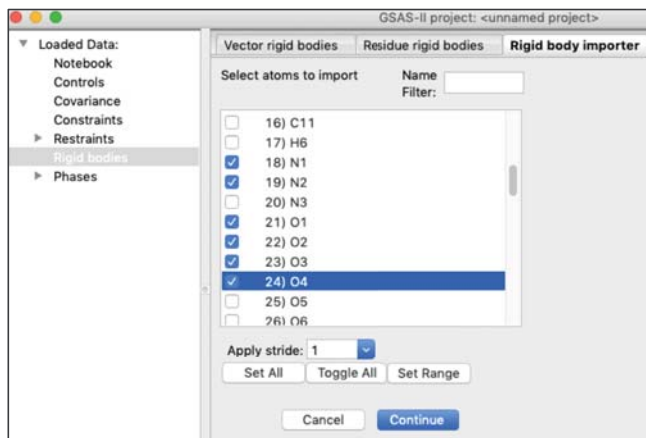
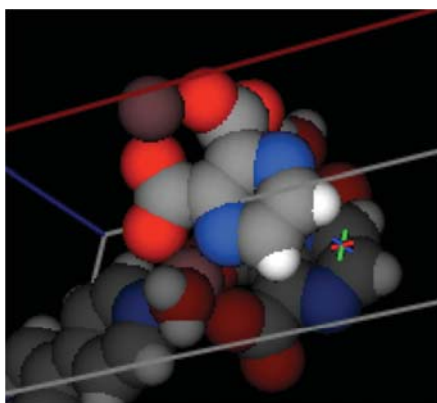


CREATE THE PYRAZINE RIGID BODY (1)

Import the CIF file again, but select different atoms

Repeating the previous process: use “Edit Vector Body”/“Extract from file” menu command again

- Select a file format (in this case CIF) and then find the CIF file and select it. Then select the 6 C atoms, 2 N and 2 H atoms and 4 O atoms in the pyrazine ion.
 - To see, it will help to reorient the 3D display by dragging with the mouse left and right buttons

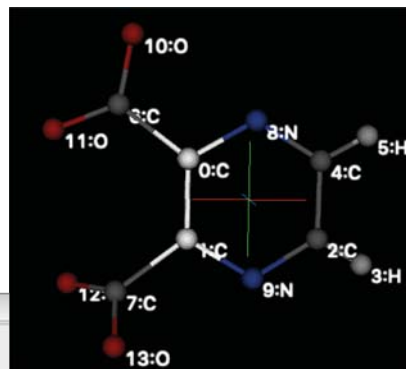


CREATE THE PYRAZINE RIGID BODY (2)

Place atoms in a plane and redefine the origin

Unselect the O atoms, since they are not planar and press “Set origin” and “Place in plane” buttons (with “xy” selected)

Select the two C atoms and press “Define as” (with “x” selected) to place the x-axis between the selected atoms



Note that these origin & axes settings are for convenience in viewing and understanding the body, but are not required.

Vector rigid bodies Residue rigid bodies **Rigid body importer**

Reorder atoms by dragging

Set All
Toggle

Reorient using selected atoms...

Set origin

Place in plane xy

Define as x

Use selected atoms to create...

a Vector Body
a Residue Body

Cancel

	Label	Select	Type	x	y	z
1	C1	<input checked="" type="checkbox"/>	C	1.06807	-0.69414	-0.00846
2	C2	<input checked="" type="checkbox"/>	C	1.07052	0.69414	0.00846
3	C3	<input type="checkbox"/>	C	-1.21613	0.68002	-0.01733
4	H1	<input type="checkbox"/>	H	-2.02415	1.13756	-0.08688
5	C4	<input type="checkbox"/>	C	-1.23793	-0.69157	0.03080
6	H2	<input type="checkbox"/>	H	-2.05011	-1.14387	0.03336
7	C5	<input type="checkbox"/>	C	2.27923	-1.61033	-0.10121
8	C6	<input type="checkbox"/>	C	2.29003	1.62459	0.03609
9	N1	<input type="checkbox"/>	N	-0.08963	-1.37842	0.07570
10	N2	<input type="checkbox"/>	N	-0.08990	1.38202	0.02947
11	O1	<input type="checkbox"/>	O	2.07147	-2.82652	0.12454
12	O2	<input type="checkbox"/>	O	3.38051	-1.14177	-0.43040
13	O3	<input type="checkbox"/>	O	3.09571	1.61361	-0.92593
14	O4	<input type="checkbox"/>	O	2.34487	2.42287	0.98654

Argonne
NATIONAL LABORATORY

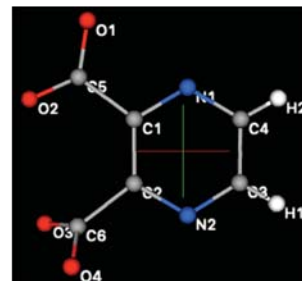
CREATE THE PYRAZINE RIGID BODY (3)

Create body & define carboxylic torsions

Since this ion needs torsional rotation for the carboxylic groups, a residue rigid body is required.

- Select all atoms and then press “a Rigid Body” to create it.
- Select the new body and rename it.
- Define two torsional degrees of freedom: (It helps to press the “Plot” button to identify the atoms.) Use Edit Rigid Body/Define torsion menu item.
 - Origin C1; Pivot C5 (riding O1 & O2)
 - Origin C2; Pivot C6 (riding O3 & O4)

Save the rigid body, if will be needed in a different project.



Edit Residue Body

Residue name: pyrazine

Orientation reference non-H atoms A-B-C: C1 C2

	Name	Type	Cart x	Cart y	Cart z
0	C1	C	1.06807	-0.69414	-0.00846
1	C2	C	1.07052	0.69414	0.00846
2	C3	C	-1.21613	0.68002	-0.01733
3	H1	H	-2.02415	1.13756	-0.08688
4	C4	C	-1.23793	-0.69157	0.03080
5	H2	H	-2.05011	-1.14387	0.03336
6	C5	C	2.27923	-1.61033	-0.10121
7	C6	C	2.29003	1.62459	0.03609
8	N1	N	-0.08963	-1.37842	0.07570
9	N2	N	-0.08990	1.38202	0.02947
10	O1	O	2.07147	-2.82652	0.12454
11	O2	O	3.38051	-1.14177	-0.43040
12	O3	O	3.09571	1.61361	-0.92593
13	O4	O	2.34487	2.42287	0.98654

Set Bond Angle Riding atoms

Del C1 C5 0.00 O1, O2

Del C2 C6 0.00 O3, O4

Selected torsion angle: 0

PREPARE TO INSERT RIGID BODIES

In this case we have a rough idea where the rigid bodies are located, so we will place them to match approximate of atoms in the structure.

Notes

- The rigid bodies have H atoms, but the atoms list does not; any rigid body atoms not in the atoms list can be added to the atoms list when the body is inserted
- There are some distortions in groups that will be corrected when atom positions are generated by from the rigid bodies.
- Note the atom list need not be ordered to match the rigid body, but that can make things more convenient.

VIEWING STRUCTURES & RIGID BODIES

The view of the structure is determined by the atoms copied from the asymmetric cell into the Draw Atoms array and their settings.

- To best view the structure and rigid body use “Stick” or “Balls & Stick” modes.
 - Select using the buttons on the RB Models tab or by double-clicking on the column labeled “style” in the “Draw Atoms” tab

The screenshot displays the software interface for viewing structures and rigid bodies. The top window shows the 'Draw Atoms' tab with a table of atoms and their settings. The 'Style' column is highlighted, and a dropdown menu is open, showing options: 'lines', 'vdW balls', 'sticks', and 'balls & sticks'. The 'sticks' option is selected. The bottom window shows a 3D molecular model of a structure, with atoms represented by spheres and bonds by sticks. The model is rendered in a stick representation, with atoms colored by element (e.g., carbon in grey, oxygen in red, nitrogen in blue).

Name	Type	x	y	z	Sym Op	Style	Label	Color	I/A
0	Co1	Co	0.14693	0.23443	1.07418	1	vdW balls		
1	C2	C	0.17598	-0.03441	1.01030	1	vdW balls		
2	C3	C	0.19689	-0.15244	1.04168	1	vdW balls		
3	C4	C	0.24874	-0.03384	1.19688	1	vdW balls		
4	C5	C	0.22855	0.08322	1.15924	1	vdW balls		
5	C6	C	0.13827	-0.00785	0.87173	1	vdW balls		
6	C7	C	0.16128	-0.28355	0.96945	1	vdW balls		
7	C8	C	0	0	0	0			
8	C9	C	0	0	0	0			
9	C10	C	0	0	0	0			
10	C11	C	0	0	0	0			
11	C12	C	0	0	0	0			
12	N13	N	0	0	0	0			
13	N14	N	0	0	0	0			
14	N15	N	0	0	0	0			
15	O16	O	0	0	0	0			
16	O17	O	0	0	0	0			
17	O18	O	0	0	0	0			

ORIENTING STRUCTURES IN WINDOW

Mouse movements change view of structure

When the structure is viewed, use of the mouse buttons changes the view of the crystal structure:

- Holding down left button (left drag): rotates axes around screen x & y
- Holding down right button (right drag): Moves the viewpoint, which is kept at the center of the screen (effectively translating the structure)
- Holding down center button (center drag): rotates axes around screen z
- Rotating the scroll wheel: changes “camera position” (zoom in/out)

When the Rigid Body and structure are shown together, holding the Alt button while dragging the mouse causes the same movements, but only to the rigid body

- Pressing the “c” key sets the viewpoint to $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ [value can also be edited in Draw Options tab]

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HIGHLIGHTING ATOMS

The “Locate and Insert Rigid Body” command creates table with rigid body atoms and matching atoms in crystal structure (with the distance between them).

Atoms can be paired.

To help determine which atoms should be paired, specific atoms can be highlighted.

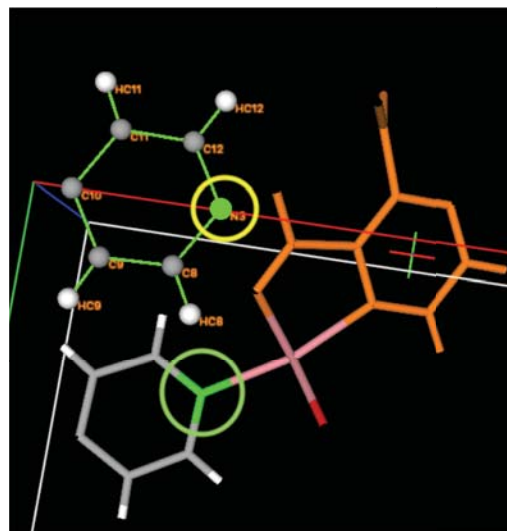
- Selecting a row causes the rigid body atom and the matching crystal structure atom to be highlighted
- To highlight a different atom in the crystal, use the “Crystal Highlight” pulldown, or press Tab to select crystal atoms
- Pressing Alt+Tab cycles through the rigid body atoms.

	RB type	phase #	phase label	delta, A	Assign as atom
C8	C	19	C12	8.127	
C9	C	18	C11	8.057	C9
C10	C	17	C10	8.985	
C11	C	15	C8	9.824	

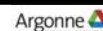
Crystal Highlight: C10

Actions with assigned atom(s)...

Process Assignments

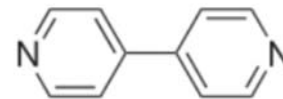


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INSERT THE BIPYRIDINE INTO THE STRUCTURE (1)

Assumes rigid body is already defined (or read in)



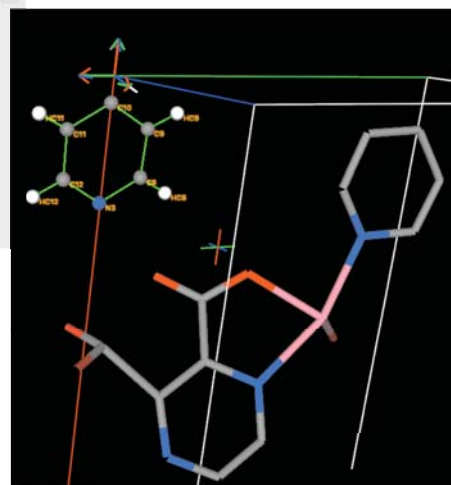
- Go to RB Models phase tab; use “Edit Body”/“Locate and Insert Rigid Body”; select the bipyridine fragment.

Edit Body	Help
Locate & Insert Rigid Body	
Auto find residues	
Copy rigid body parms	
Global thermal motion	
Global residue refine	
Remove all rigid bodies	

RB type	phase #	phase label	delta, Å	Assign as atom
C8	11	C6	6.615	
C9	5	C12	7.754	
C10	4	C11	8.073	
C11	12	C7	7.877	
C12	7	C2	7.756	
N3	13	N13	8.281	
HCB			-1.7	-1.000 Create new
HCB9			-1.7	-1.000 Create new
HC11			-1.7	-1.000 Create new
HC12			-1.7	-1.000 Create new

Note that the crystal structure is shown as the stick diagram; the rigid body is shown as balls & green sticks

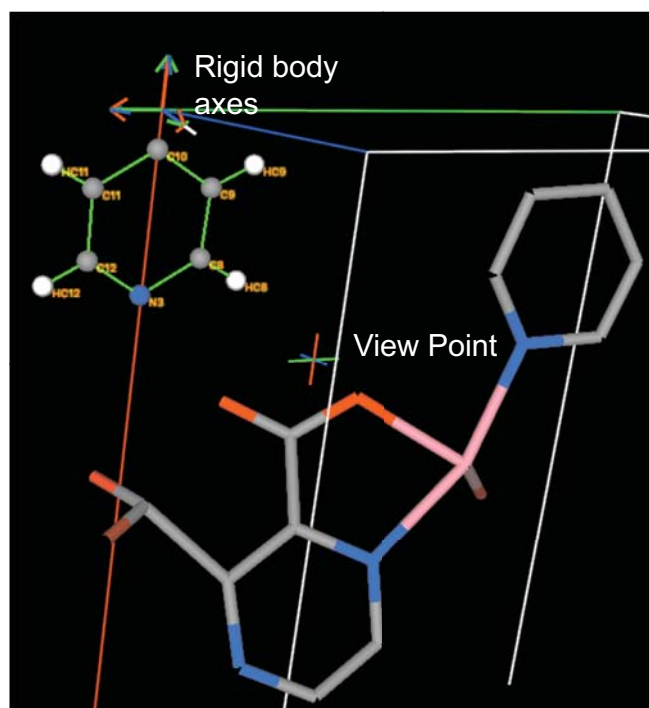
Also, the rigid body has H atoms, the crystal structure does not; H atoms will be added to structure (noted as “Create new” in table) since they can’t be matched



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WHAT IS SHOWN IN STRUCTURE PLOT

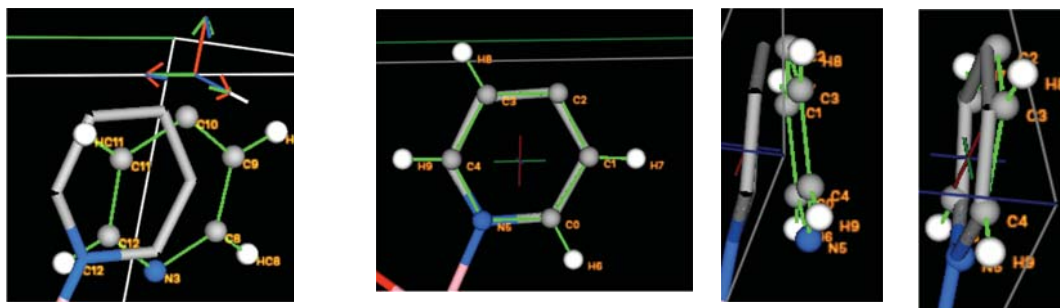
- The View Point (six-line star) shows the cell axes. Move with right mouse; reset to $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ with “c”
- The triplet with arrows shows the Cartesian axes with the origin placed the rigid body position
- Axes & cell edges are colored red, green & blue for x, y & z, respectively
- The white line in the triplet is the vector direction for the rigid body orientation. The azimuth angle rotates the rigid body around this axis.



INSERT THE BIPYRIDINE INTO THE STRUCTURE (2)

Position RB close to location in structure

- Use mouse to reorient view of structure
- Holding Alt down & use of Left/Middle/Right repositions the rigid body.
- As noted before: bipyridine origin must be at $\bar{1}$
- Edit origin to enter $(0, \frac{1}{2}, 1)$ (N.B. RB is now close as shown below)
 - Press lock to prevent changing this by accident with Alt+right mouse
- Use Alt+Left & Alt+Middle to get bodies close; rotating plot for multiple views



Note that as the atoms are moved, the table is updated with the closest matches between atoms and the distances between them.

Locating rigid body : halfBiPy Display crystal structure as: Ball & Sticks Sticks

Origin: x 0.0 y 0.5 z 1.0 Lock

Orientation azimuth: 180.0

Orientation vector x: 0.0058 y: 0.0 z: 0.1347 (frac coord)

Rigid body symmetry axis: None x y z x+y x+y+z

No side chain torsions

Add Cancel

Match between atoms in rigid body and crystal. Use assignments to align bodies.

RB type	phase #	phase label	delta, A	Assign as atom	Crystal Highlight:
C8	1	C8	1.374		
C9	2	C9	1.816		
C10	3	C10	1.837		
C11	4	C11	1.377		
C12	5	C12	0.838		
N3	6	N15	1.848		
H8	-1 ?	-1.000	Create new		
H9	-1 ?	-1.000	Create new		
H11	-1 ?	-1.000	Create new		
H12	-1 ?	-1.000	Create new		

Actions with assigned atom(s)...

Process Assignments

Set Origin

Set Orientation

Set both

INSERT THE BIPYRIDINE INTO THE STRUCTURE (3)

RB has been located close to site in structure

- Adjust until all non-H atoms match within $\sim 0.2\text{\AA}$
- Press "Add" to use use this origin and orientation.

The window changes to show the rigid body parameters. Rigid body bonds are shown in Orange (by default)

General Data Atoms Draw Options Draw Atoms RB Models Map peaks

Residue rigid bodies:

halfBiPy:0

Name: halfBiPy:0 Delete

Origin x,y,z (frac) 0.0 0.5 1.0 Refine?

Rotation angle (deg) & Orient. vector (frac) 150.14 0.0044 -0.0046 0.1344

Rigid body thermal motion model: None Units: T A², L deg², S deg-A

General Data Atoms Draw Options Draw Atoms RB Models Map peaks

Locating rigid body : halfBiPy Display crystal structure as: Ball & Sticks Sticks

Origin: x 0.0 y 0.5 z 1.0 Lock

Orientation azimuth: 150.14

Orientation vector x: 0.0044 y: -0.0046 z: 0.1344 (frac coord)

Rigid body symmetry axis: None x y z x+y x+y+z

No side chain torsions

Add Cancel

Match between atoms in rigid body and crystal. Use assignments to align bodies.

RB type	phase #	phase label	delta, A	Assign as atom	Crystal Highlight:
C8	1	C8	0.198		
C9	2	C9	0.058		
C10	3	C10	0.152		
C11	4	C11	0.169		
C12	5	C12	0.109		
N3	6	N15	0.098		
H8	-1 ?	-1.000	Create new		
H9	-1 ?	-1.000	Create new		
H11	-1 ?	-1.000	Create new		

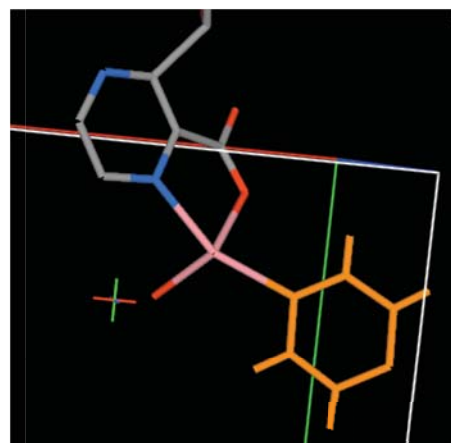
Actions with assigned atom(s)...

Process Assignments

Set Origin

Set Orientation

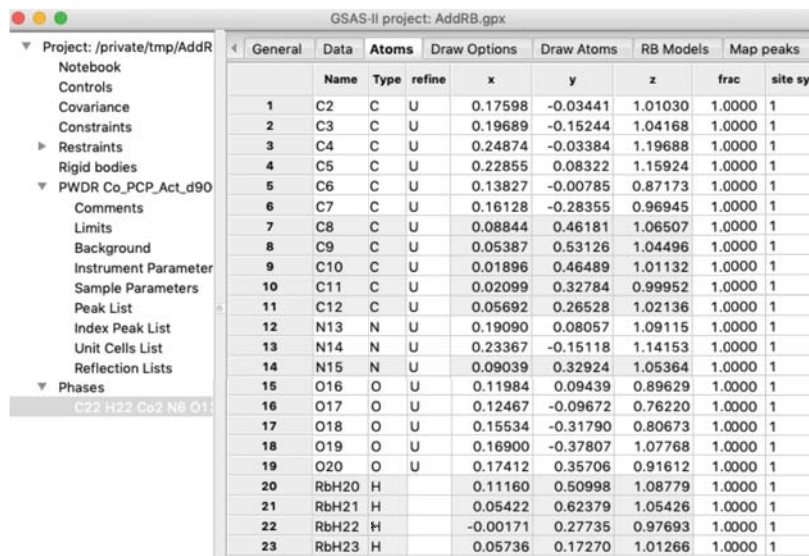
Set both



CHANGE IN THE ATOMS TABLE

Atoms in the rigid body are displayed in gray

- After the rigid body is added, atoms in rigid bodies are highlighted in gray in the atoms display.
 - Note that atoms added to the list when the RB was included are name “Rb...” and are placed at the end of the list.



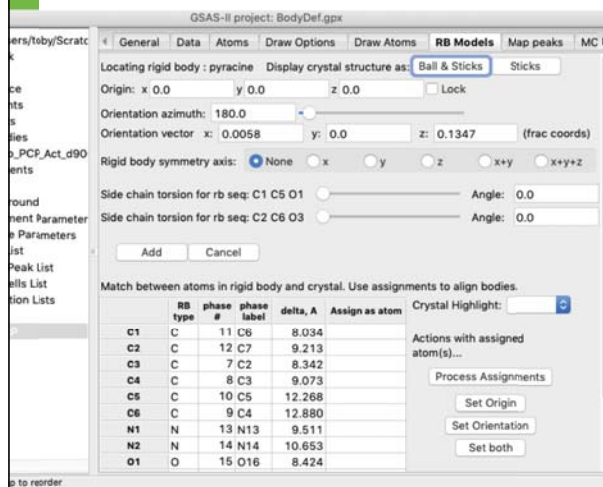
	Name	Type	refine	x	y	z	frac	site syr
1	C2	C	U	0.17598	-0.03441	1.01030	1.0000	1
2	C3	C	U	0.19689	-0.15244	1.04168	1.0000	1
3	C4	C	U	0.24874	-0.03384	1.19688	1.0000	1
4	C5	C	U	0.22855	0.08322	1.15924	1.0000	1
5	C6	C	U	0.13827	-0.00785	0.87173	1.0000	1
6	C7	C	U	0.16128	-0.28355	0.96945	1.0000	1
7	C8	C	U	0.08844	0.46181	1.06507	1.0000	1
8	C9	C	U	0.05387	0.53126	1.04496	1.0000	1
9	C10	C	U	0.01896	0.46489	1.01132	1.0000	1
10	C11	C	U	0.02099	0.32784	0.99952	1.0000	1
11	C12	C	U	0.05692	0.26528	1.02136	1.0000	1
12	N13	N	U	0.19090	0.08057	1.09115	1.0000	1
13	N14	N	U	0.23367	-0.15118	1.14153	1.0000	1
14	N15	N	U	0.09039	0.32924	1.05364	1.0000	1
15	O16	O	U	0.11984	0.09439	0.89629	1.0000	1
16	O17	O	U	0.12467	-0.09672	0.76220	1.0000	1
17	O18	O	U	0.15534	-0.31790	0.80673	1.0000	1
18	O19	O	U	0.16900	-0.37807	1.07768	1.0000	1
19	O20	O	U	0.17412	0.35706	0.91612	1.0000	1
20	RbH20	H		0.11160	0.50998	1.08779	1.0000	1
21	RbH21	H		0.05422	0.62379	1.05426	1.0000	1
22	RbH22	H		-0.00171	0.27735	0.97693	1.0000	1
23	RbH23	H		0.05736	0.17270	1.01266	1.0000	1



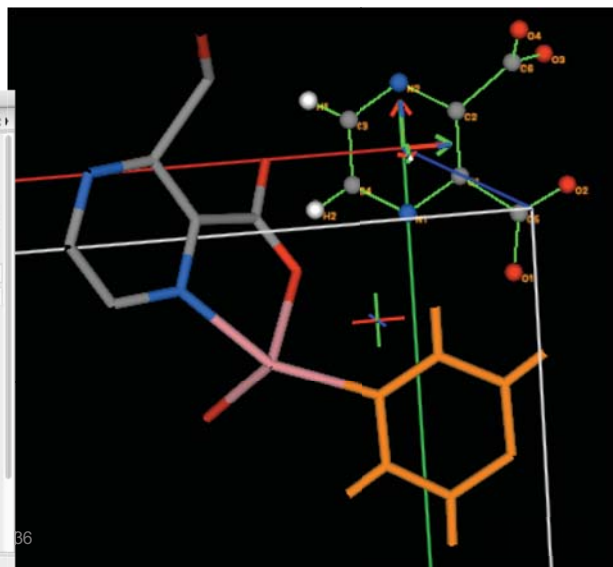
INSERT THE PYRAZINE INTO THE STRUCTURE (1)

Identify the body

- Go to RB Models phase tab; use “Edit Body”/“Locate and Insert Rigid Body”; select the pyrazine fragment
- Note that for this body, both the origin and orientation must be determined.



RB type	phase #	phase label	delta, A	Assign as atom
C1	11	C6	8.034	
C2	12	C7	9.213	
C3	7	C2	8.342	
C4	8	C3	9.073	
C5	10	C5	12.268	
C6	9	C4	12.880	
N1	13	N13	9.511	
N2	14	N14	10.653	
O1	15	O16	8.424	



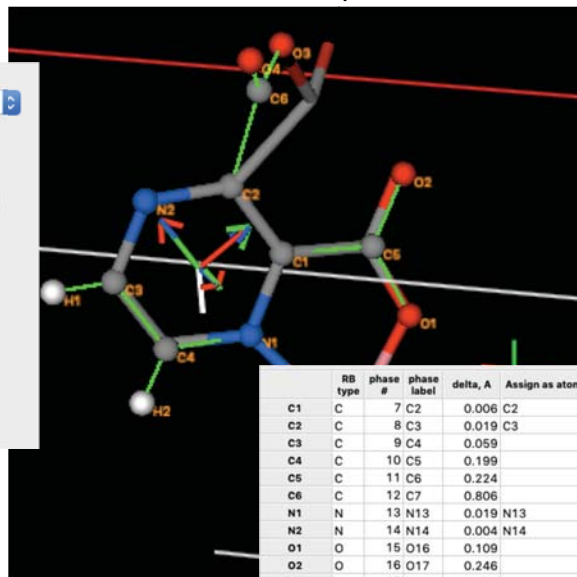
INSERT THE PYRAZINE INTO THE STRUCTURE (2)

Define pairs of atoms

- This time we will identify rigid atoms that should be paired with specific atoms in the structure. We will use the 1st two C and 1st two N atoms. Then press the “Set both” button for a best-fit.

Match between atoms in rigid body and crystal. Use assignments to align bodies.

	RB type	phase #	phase label	delta, A	Assign as atom	Crystal Highlight: C2
C1	C	7	C2	5.200	C2	
C2	C	8	C3	5.619	C3	
C3	C	11	C6	5.758	Co1	
C4	C	12	C7	7.503	C2	
C5	C	10	C5	6.210	C4	
C6	C	9	C4	6.763	C3	
N1	N	13	N13	6.819	C4	
N2	N	14	N14	7.818	C5	
O1	O	15	O16	3.237	C6	
O2	O	16	O17	2.835	C7	
O3	O	17	O18	3.747	N13	
O4	O	18	O19	3.928	N14	
H1	H	-1	?	-1.000	O16	
H2	H	-1	?	-1.000	O17	



RB type	phase #	phase label	delta, A	Assign as atom
C1	C	7 C2	0.006	C2
C2	C	8 C3	0.019	C3
C3	C	9 C4	0.059	
C4	C	10 C5	0.199	
C5	C	11 C6	0.224	
C6	C	12 C7	0.806	
N1	N	13 N13	0.019	N13
N2	N	14 N14	0.004	N14
O1	O	15 O16	0.109	
O2	O	16 O17	0.246	
O3	O	17 O18	0.728	
O4	O	18 O19	0.571	
H1	H	-1 ?	-1.000	Create new
H2	H	-1 ?	-1.000	Create new

With 4 sets of atoms paired an excellent alignment is obtained

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INSERT THE PYRAZINE INTO THE STRUCTURE (3)

Adjust torsions

- The torsions set at 0 degrees reproduces the initial structure well, but moving the sliders shows different options.
- Press the “Add” button to insert this body.

General Data Atoms Draw Options Draw Atoms **RB Models** Map peaks MC

Locating rigid body: pyrazine Display crystal structure as: Ball & Sticks Sticks

Origin: x: 0.21216 y: -0.03513 z: 1.112 Lock

Orientation azimuth: 212.46

Orientation vector: x: -0.0034 y: -0.0009 z: 0.1279 (frac coords)

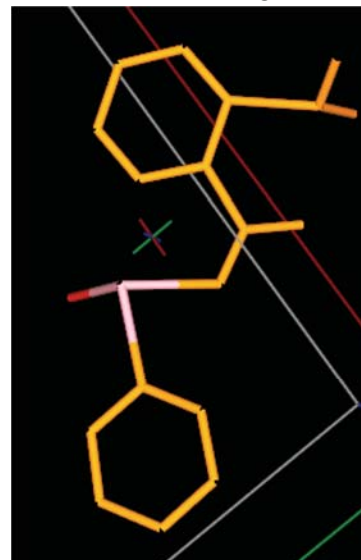
Rigid body symmetry axis: None x y z x+y x+y+z

Side chain torsion for rb seq: C1 C5 C4 C3 Angle: 0.0

Side chain torsion for rb seq: C2 C6 C5 C4 Angle: 0.0

Add Cancel

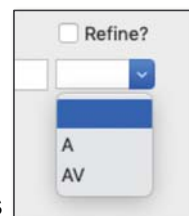
Bonds in rigid bodies are shown as orange lines in stick or ball-and-stick plots



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REFINEMENT WITH RIGID BODIES

Orientation and Origin can be refined



Origin: The rigid body origin can be refined or not. (In special cases it may be necessary to use a “Hold” constraint on one or two origin parameters – see next slide.)

Orientation: orientation is defined by a quaternion, reorganized as a unit vector and azimuthal rotation around that vector.

Orientation can be refined in one of two modes: “A” or “AV”.

- In “AV” mode, both the vector and azimuth are refined
- In “A” mode, only azimuthal rotation is refined. This is used when symmetry requires a particular orientation for the vector.

Example: For bipyridine, the origin cannot be refined, but for pyrazine it should be. For both, the orientation can be refined as “AV”

SYMMETRY SPECIAL CASES FOR RIGID BODIES

Constraints on the Rigid Body Cartesian & Crystal origin/axes

- **Center of symmetry:** The Cartesian origin will need to be the -1 position. This always(?) will be either on an atom or at the midpoint between two atoms. Usually only one from each symmetry-related pair of atoms will be included in the body (or occupancies must be set to 0.5 due to atom duplication).
 - Crystal coordinates: The rigid body origin will be fixed as the -1 site. No constraints on orientation.
- **Mirror plane:** The normal to the mirror plane must be along a fixed Cartesian axis* and the Cartesian origin must fall in the plane. (E.g. if z is unique then the plane must be at z=0).
 - Crystal coordinates: One coordinate in the rigid body origin will need to be fixed on the mirror plane (place a hold on variable $p::RBRP\xi:## \xi=x, y \text{ or } z$). The RB orientation vector will need to be fixed along the mirror plane normal. The RB azimuth angle can be refined.
- **Rotation axis:** The Cartesian origin must be on the axis, which will be at a midpoint between a group of atoms or on an atom. Align the axis along a fixed Cartesian axis* .
 - Crystal coordinates: coordinates for the rigid body origin will need to be constrained to stay on the axis by placing holds and/or constraints on origin parameters ($p::RBRP\xi:## \xi=x, y \text{ or } z$) to leave one free parameter. The RB orientation vector will need to be fixed along the axis. The RB azimuth angle can be refined.

Glide planes and screw axes will require constraints similar to above only when the symmetry is internal to the molecular fragment (not common).

* Fixed Cartesian axes are x, y, z, x+y or x+y+z 40

INSERTING THE RIGID BODY: SYMMETRY SETTINGS

For bodies on mirror planes or rotation axes

- When inserting a body with azimuthal symmetry constraints, the axis previously defined as the symmetry axis must be designated

The screenshot shows a software interface for inserting a rigid body. The title is "Locating rigid body : pyracine". There are two buttons for "Display crystal structure as": "Ball & Sticks" and "Sticks". Below this, there are input fields for "Origin: x 0.0", "y 0.0", and "z 0.0", along with a "Lock" checkbox. The "Orientation azimuth:" is set to "187.9" with a slider. The "Orientation vector" is shown as "x: 1.0", "y: 0.0", and "z: 0.0" in "frac coords". At the bottom, the "Rigid body symmetry axis:" is set to "z", with radio buttons for "None", "x", "y", "z", "x+y", and "x+y+z". A yellow box highlights the "z" radio button and its label.

- The orientation vector will need to be specified as well as the origin.
- The effect of rigid body angular rotation can be viewed with the azimuth slider

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ADP FITTING FOR RIGID BODIES

ADP = Atomic Displacement Parameters (~ thermal parameters)

Motion of rigid bodies can be described by ADPs for individual atoms or with terms that describe the possible motion associated with a rigid group of atoms. These are known as TLS terms.

- The T terms describe translational motion, which will be the same for all atoms in the group, but can differ by direction.
- The L terms describe libration, which can be thought of as frustrated rotations around the origin of the body. The further the atom is located from the body origin, the larger L will make the ADP.
- The S terms describe “screw” motion, which combines T & L motion, and is not needed if the group motion is unhindered and origin is at the center of mass.

The simplest ADP model for a rigid body is to constrain all atoms in the group to have the same Uiso value. The next most complex model is to have a single T ($T_{11}=T_{22}=T_{33}$) & single L term ($L_{11}=L_{22}=L_{33}$). I sometimes use a few T & L terms, but never more than that (with powder data).

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OTHER RIGID BODY TRICKS

- It can be useful to combine restraints with rigid body constraints. For the example structure, restraints can be placed on the Co-O and Co-N bond distances, which places further restrictions to prevent the refinement from overfitting.
- Rigid Body torsions will not move H atoms as riders. If H atoms are needed, use Edit Atoms/"on selected atoms..."/"Calc H atoms" to generate H atoms on riders.
- On occasion I have needed to have two rigid bodies that have a fixed connection with each other, but still have degrees of freedom. To do that in GSAS/EXPGUI, I define the bodies so that they share an origin at the point which joins them. I then constrain the origin of the two groups to refine together. This is probably not needed in GSAS-II, since both groups of atoms can be placed in a single body with a torsion between them.

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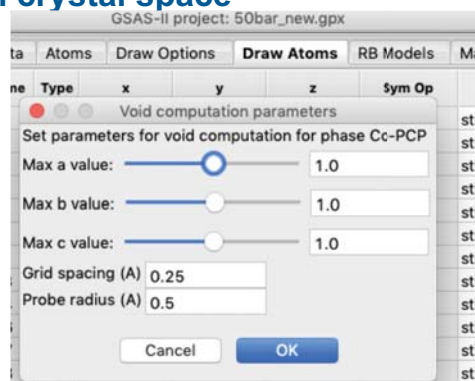
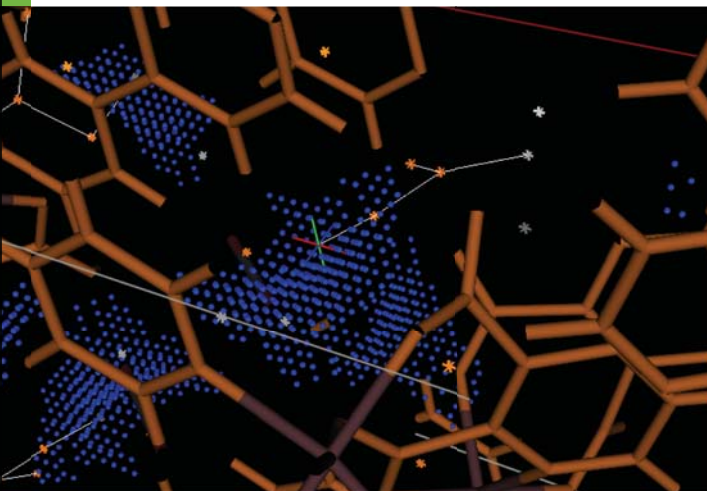


OTHER NICE TOOLS FOR GUEST/SOLVENT MOLECULE STRUCTURES

Understanding the spatial environment in crystal space

Void space visualizer: "Edit Figure"/"Create Void Map" (in Draw Atoms)

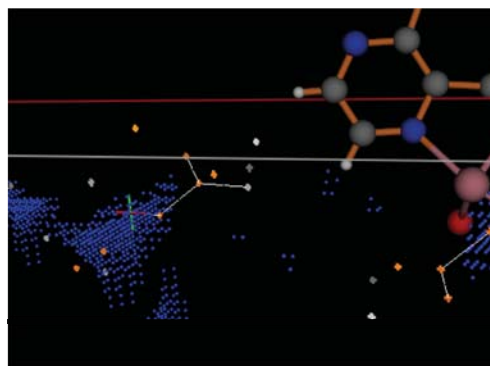
- Resulting map shows regions of space without atoms



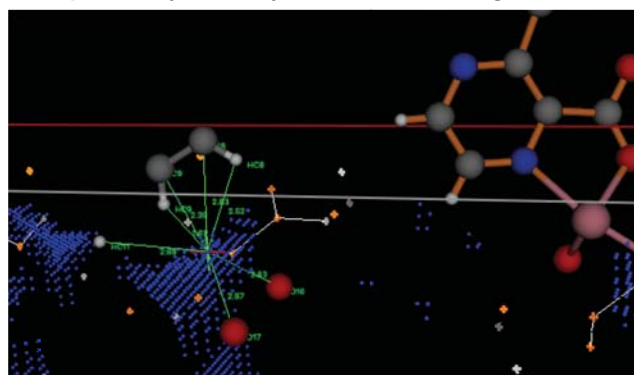
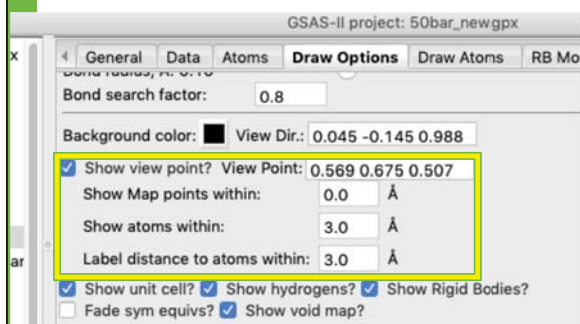
OTHER NICE TOOLS FOR GUEST/SOLVENT MOLECULE STRUCTURES

Using the View Point

- By default, the view point is set to $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$
- Move view point using right mouse button
 - Movement in in screen x-y
 - Rotate drawing (left mouse) for 3rd dimension
 - Position is shown in bottom frame
 - Reset to $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ by pressing "c" key
 - Type in coordinates on Draw Options
- Optionally, highlight distances around view point; symmetry-related atoms generated



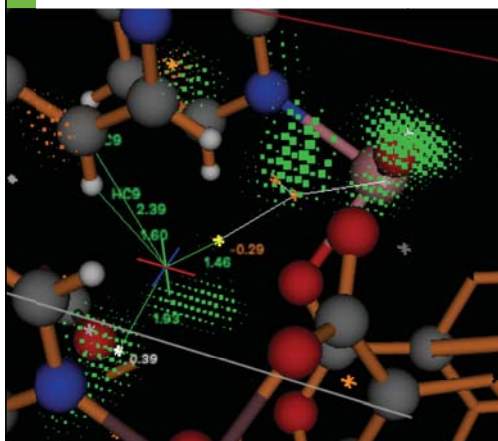
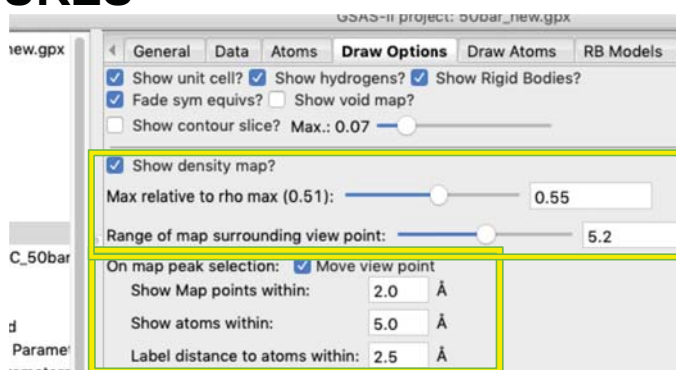
view point: 0.4287, 0.3024, 0.4885; density: 0.2312



OTHER NICE TOOLS FOR GUEST/SOLVENT MOLECULE STRUCTURES

New feature: understand Fourier map peaks

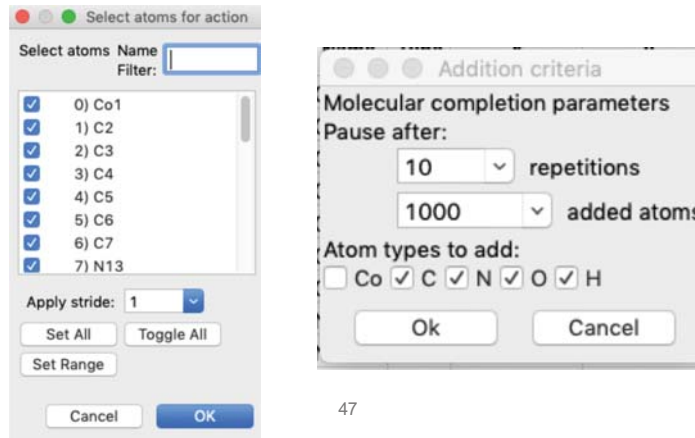
- Highlight distances around a selected Fourier map peak
- Note distances are labeled as set in Draw Options
- Also, optionally show map



	mag	x	y	z	dzero	dcent
0	0.5149	0.3264	0.8958	0.5938	14.5724	7.4065
1	0.4117	0.6528	0.2500	0.5000	22.6040	5.9093
2	0.3946	0.6042	0.0833	0.5938	20.8103	5.5045
3	0.3908	0.5556	0.5833	0.5312	19.9927	2.0900
4	0.2808	0.4167	0.2500	0.4375	14.5648	3.8091
5	0.2654	0.3056	0.1250	0.4062	10.6416	7.6950
6	0.2675	0.6310	0.8958	0.6562	23.5303	6.0384

A FEW OTHER NEW VISUALIZATION/MAP FEATURES

- Map peaks (Map peaks menu)
 - Equivalent peaks: finds peaks related by symmetry to a selected peak
 - Unique Peaks: brings one symmetry-unique peak to top of list
- Draw Atoms (Edit Figure menu)
 - Complete Molecule: Adds atoms bonded to selected atoms already in draw list



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CONCLUSIONS

Rigid bodies are fun, perhaps not easy, but very useful

GSAS-II has two very powerful rigid body implementations

New GSAS-II tools make them much easier to create and use